

# Looking back: how far have we come?

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with materials from Calistus Ngonghala

# Genesis



## ***E<sup>2</sup>M<sup>2</sup>: Ecological and Epidemiological Modeling in Madagascar***

January 13-20 & January 22, 2018

Centre ValBio, Ranomafana National Park & Institut Pasteur de Madagascar, Antananarivo

***Applications available at:***

**<http://metcalflab.princeton.edu/e2m2-application/>**

**Deadline: Wednesday, November 1, 2017**

We are pleased to announce the second annual *E<sup>2</sup>M<sup>2</sup>: Ecological and Epidemiological Modeling in Madagascar* clinic, to be held January 13-20, 2018 at Centre ValBio, Ranomafana National Park, Madagascar, with a mandatory closing session to follow at Institut Pasteur de Madagascar on January 22. The clinic will be a ten-day intensive workshop aimed to provide an introduction to the use of dynamical models in understanding ecological and epidemiological data.

Students will participate in a series of interactive lectures and computer-based tutorials and learn to fine-tune model-based research questions, develop clear model frameworks and corresponding equations, and fit models to real-world data. All students will work closely with peers and faculty to develop a research plan for an ongoing or existing project integrating dynamical modeling with data collection and/or analysis in a

# Outline

- Research question and interest
- Mechanistic model
- Statistical model
- R

# Research question

## Abstract

**Title: "Modeling polymerization of branched actin filaments"**

In this project we will construct Master equations and Fokker Planck equations for the stochastic process of the (de)polymerization of actin filaments. The basic case of a single straight filament with simplified dynamics was considered in class during the biological physics course. This project will extend this case to consider multiple (de)polymerizing filaments, stochastic nucleation of new filaments and filament branches. Where possible, the stochastic differential equations will be solved analytically. When this is not possible we will solve the equations numerically. The results will be compared to data from biochemistry experiments and stochastic simulations done by member of the team at the University of Sheffield.



# Research question

How...? = mechanistic model

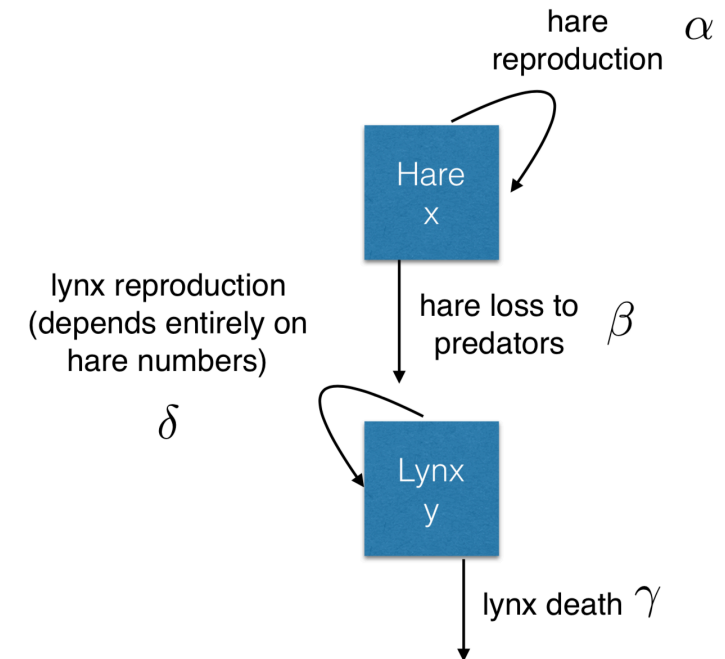
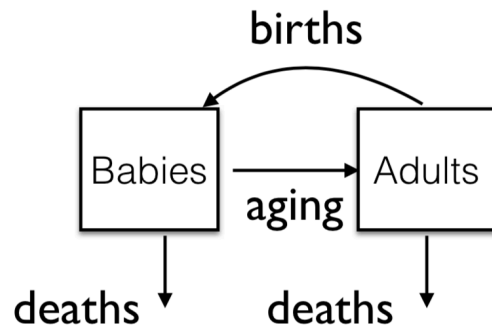
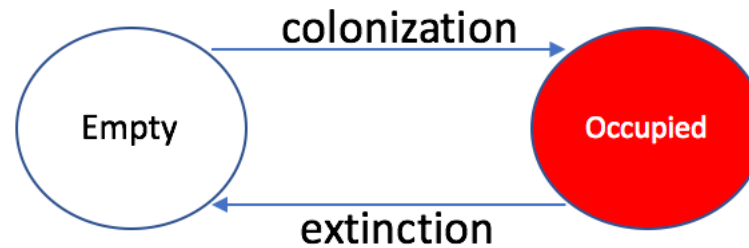
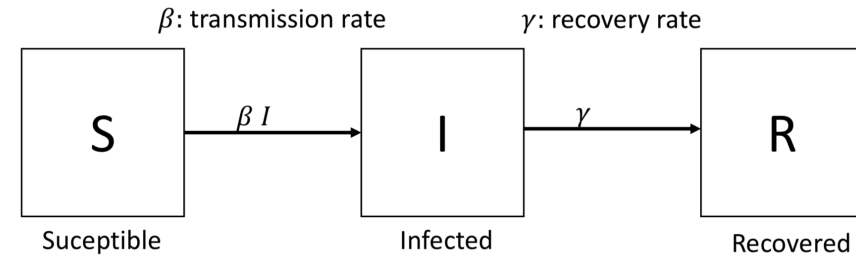


Does...? = statistical model

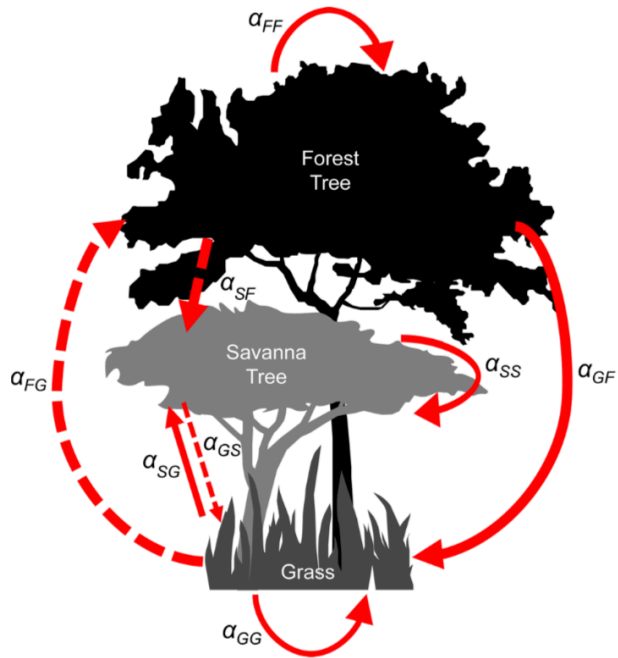


# Mechanistic model: process-driven

- Compartmental model
- State: box
- Process: arrow



# Equivalence?



$$\frac{dS}{dt} = r_S S (1 - \alpha_{SG} G - \alpha_{SF} F - \alpha_{SS} S) + \xi_1$$

$$\frac{dF}{dt} = r_F F (1 - \alpha_{FG} G - \alpha_{FF} F) + \xi_2$$

$$\frac{dG}{dt} = r_S G (1 - \alpha_{GS} S - \alpha_{GF} F - \alpha_{GG} G) + \xi_3$$

**Figure 1.** A pictorial representation of the model. *Thicker arrows* represent stronger limitation (larger competition coefficient values). The pathway of *different dashed arrows* represents a potential opportunity for savannas to facilitate their own growth via reduced limitation on grasses, which repels forest trees. For parameter definitions, see Table 1.

The model is a formulation of the classic Lotka–Volterra competition model, with notation following Chesson (2000). The model aims to capture the dynamics of vegetation in areas with annual precipitation ranging from about 800–2000 mm, where savanna and forest potentially constitute alternative self-reinforcing states maintained primarily through differences in fire dynamics (for example, Sankaran and others 2005; Staver and others 2011). The model has three functional groups: grasses (G), savanna trees (S), and forest trees (F), and their abundance is expressed in terms of vegetation cover per unit ground at the spatial resolution of an area that would fit one fully grown forest tree and multiple individual grasses. We assume that cover is proportional to the size of a single tree in this patch. Together, the three groups do not necessarily sum to 100%, because vegetation can have multiple, overlapping layers and systems with more species often achieve greater biomass/cover than monocultures, through complementary use of resources or other mechanisms (Tilman and others 2014).

The dynamics of these three functional groups are given by the following three equations:

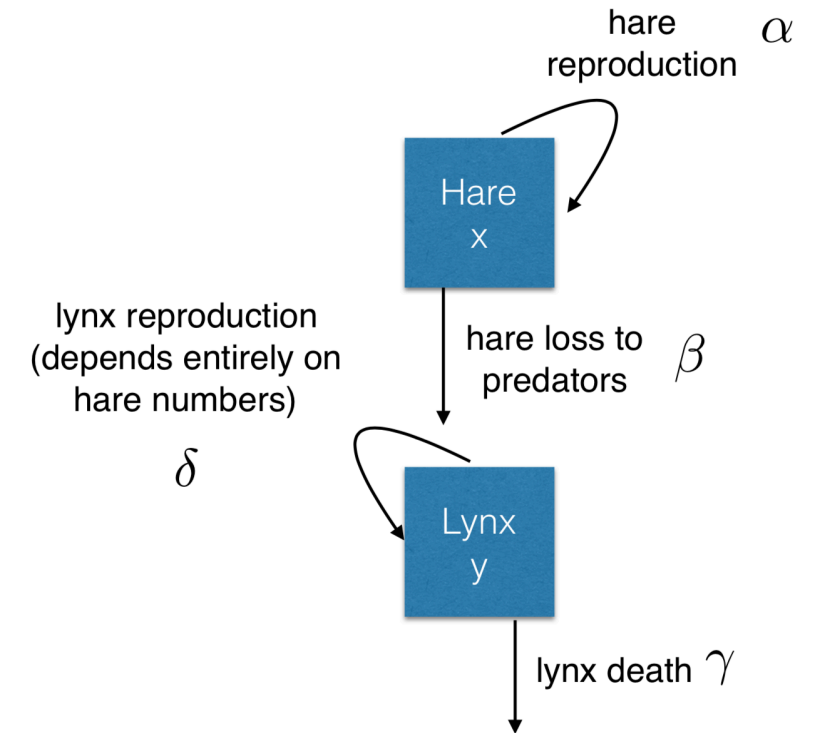
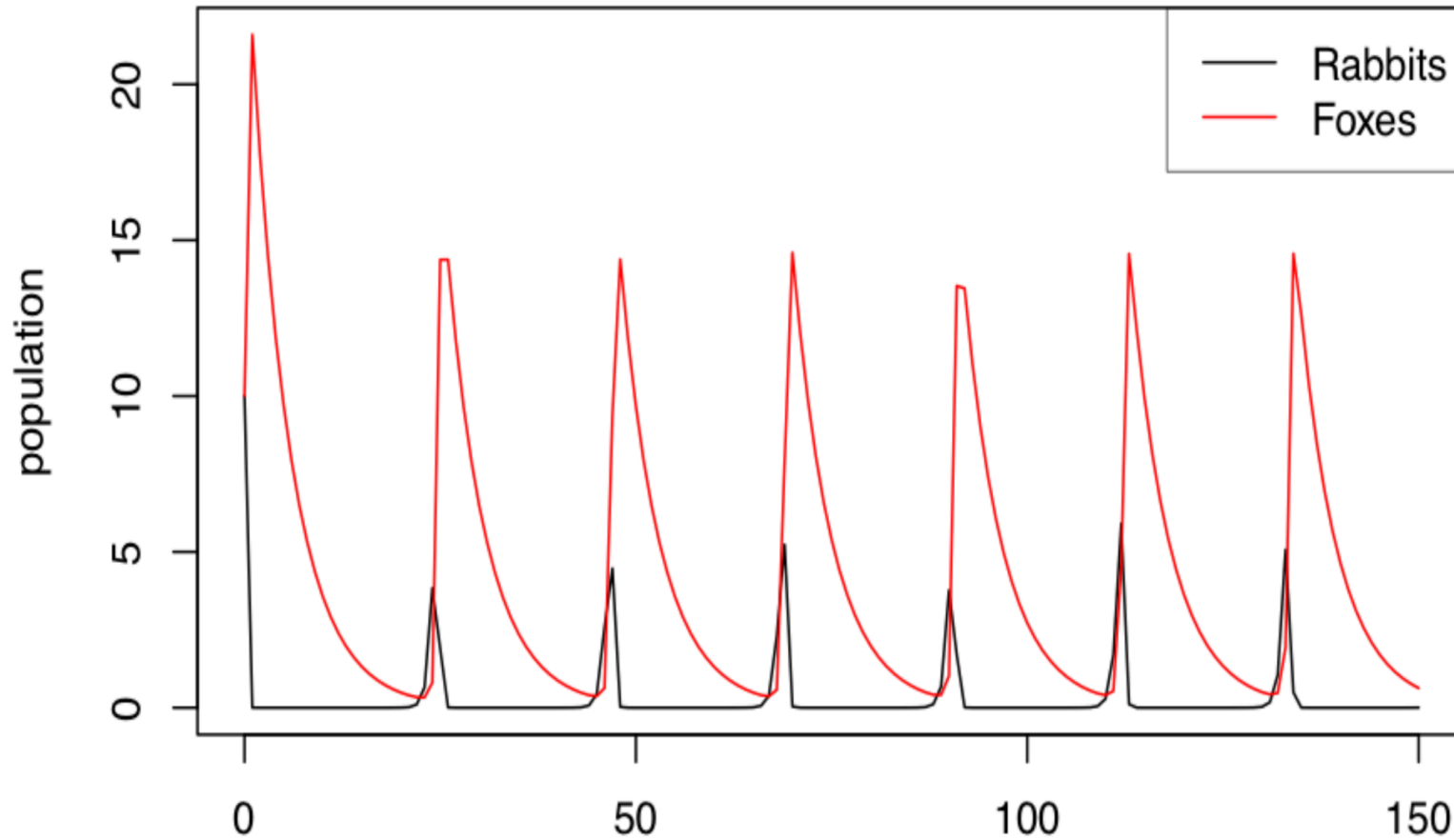
$$\frac{dS}{dt} = r_S S (1 - \alpha_{SG} G - \alpha_{SF} F - \alpha_{SS} S) + \xi_1$$

$$\frac{dF}{dt} = r_F F (1 - \alpha_{FG} G - \alpha_{FF} F) + \xi_2$$

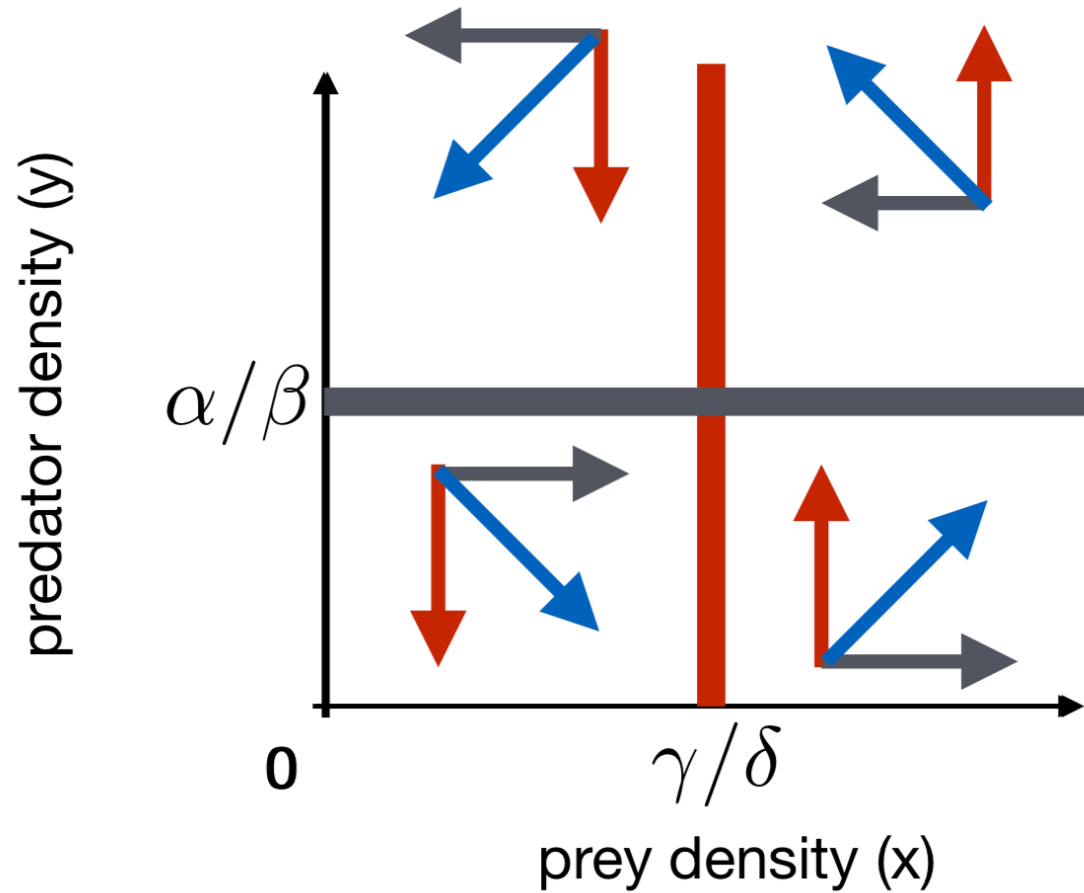
$$\frac{dG}{dt} = r_S G (1 - \alpha_{GS} S - \alpha_{GF} F - \alpha_{GG} G) + \xi_3$$

$r_S$ ,  $r_F$ , and  $r_G$  are maximum growth rates.  $\alpha_{ij}$  are competition coefficients, representing the competitive effect of species  $j$  on species  $i$ , with larger values indicating that species  $j$  reduces species  $i$ 's growth more. The  $\alpha_{ii}$  coefficients, therefore, are self-limitation coefficients that can be interpreted as  $1/\text{carrying capacity}$ . Each equation is also driven by independent additive Gaussian white noise  $\xi_{1-3}$ , accounting for sources of uncertainty associated with disease, herbivory, resource variability, and other stochastic factors (for example, Ridolfi and others 2011).

# Analyses: forward simulation



# Analyses: phase plane



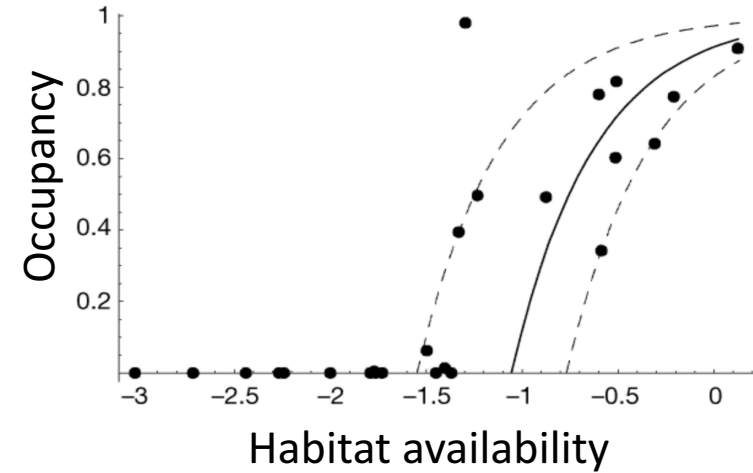
# Analyses: equilibrium

- Equilibria

$$\begin{aligned}\frac{dp}{dt} = 0 &\iff cp(1-p) - ep = 0 \\ &\iff p^* = 0 \text{ or } p^* = 1 - \frac{e}{c}\end{aligned}$$

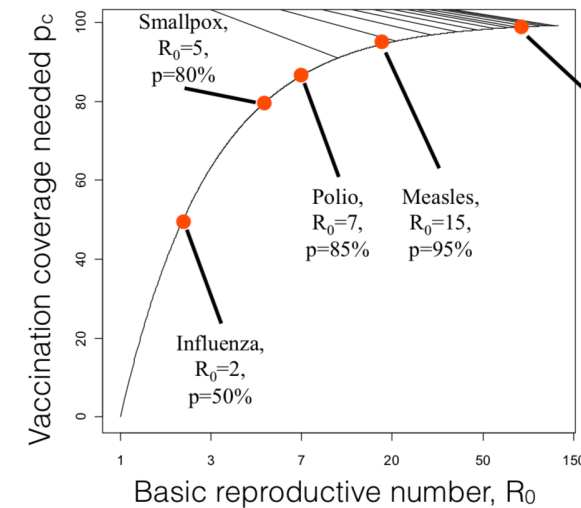
# Insights

- Exponential increase
- Cyclic dynamic
- Extinction threshold
- Basic reproductive number  $R_0$
- Effective reproductive number  $R_E$
- Vaccination cover  $p_c$
- ...



Hanski & Ovaskainen, 2000, *Nature*

Same logic as without births:  $p_c = 1 - \frac{1}{R_0}$



More transmissible diseases are harder to eradicate

# Families of models

Discrete models

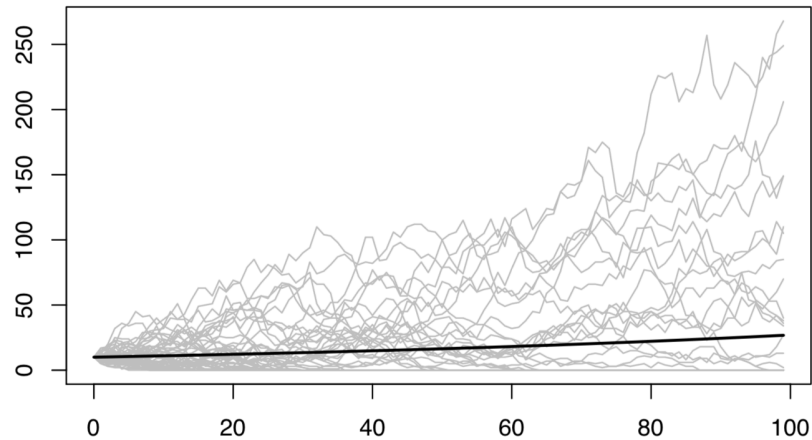
## Structured population model

$$\mathbf{n}_{t+1} = \mathbf{A} \mathbf{n}_t$$

Continuous models

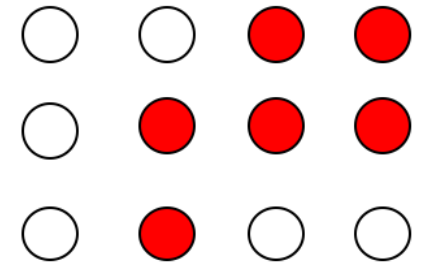
$$\begin{aligned}\frac{dS(t)}{dt} &= -\beta S(t)I(t) \\ \frac{dI(t)}{dt} &= \beta S(t)I(t) - \gamma I(t) \\ \frac{dR(t)}{dt} &= \gamma I(t)\end{aligned}$$

Deterministic and stochastic models

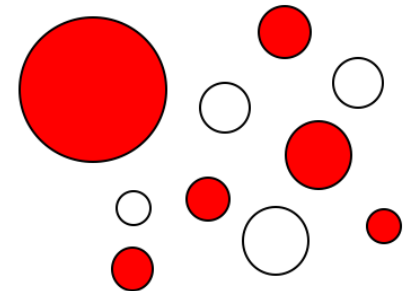


Spatial models

Spatially implicit: homogenous



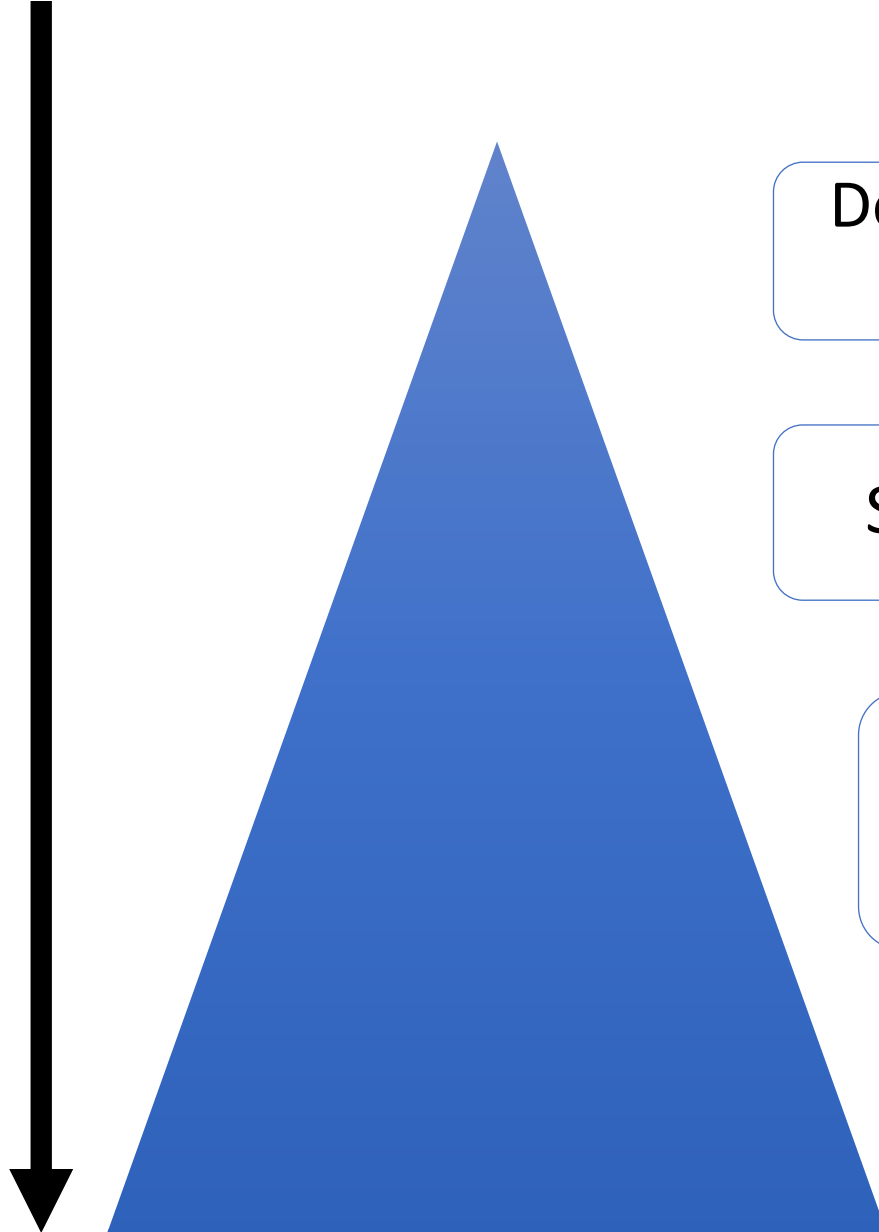
Spatially realistic: heterogeneous





# Degree of complexity

Increasing complexity and realism  
Decreasing tractability



Deterministic models

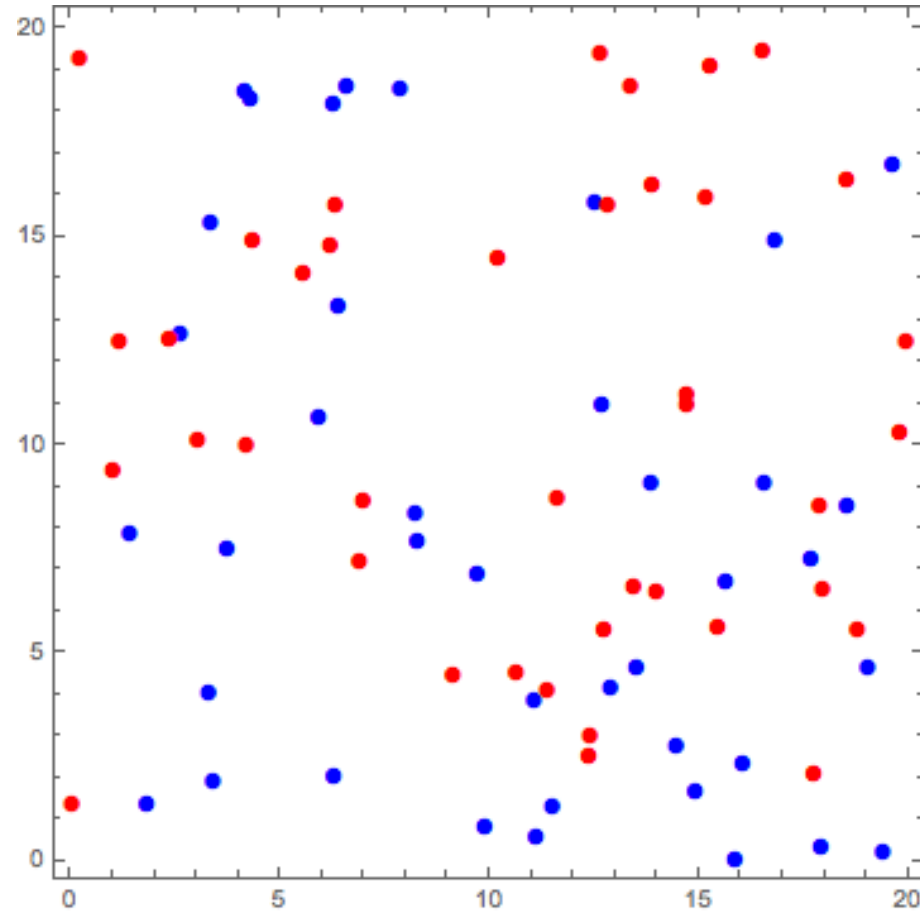
(Continuous/Discrete)

Stochastic models

Meta-population/  
Network

Agent-based

# Agent based: continuous landscape



# Outline

- Science: research question
- Mechanistic model
- Statistical model
- R

# Statistical modeling: **data**-driven



POSITIVE PROOF OF GLOBAL WARMING

Correlation does not imply causation

# Regression families and assumptions

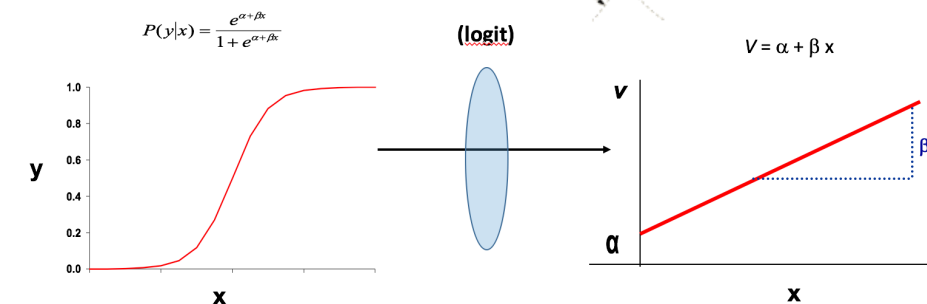
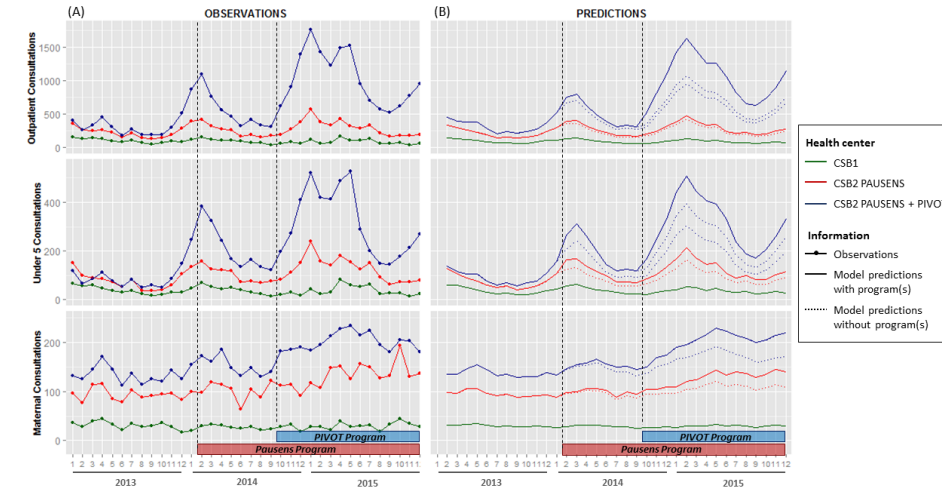
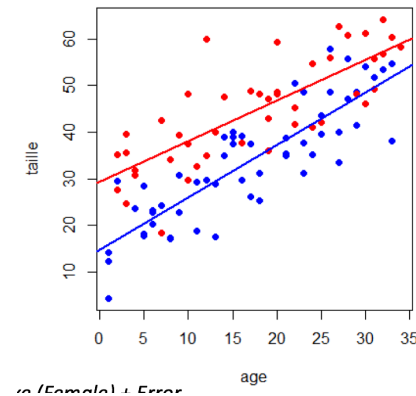
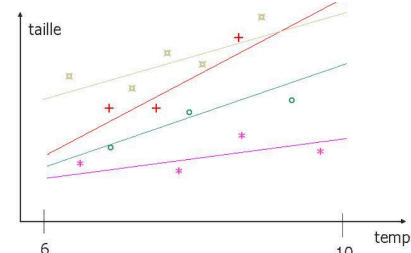
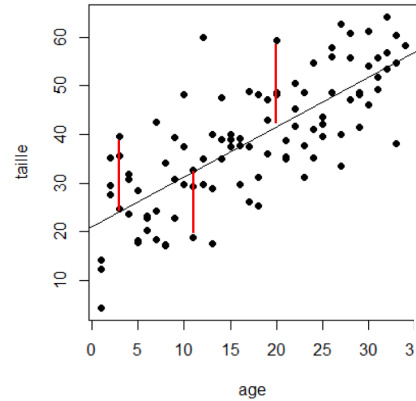
1. Univariate Linear Models

2. Multivariate Linear Models

3. Generalized Linear Models

4. Generalized Linear Mixed Models

5. Evaluating trends and effects over time



# Occupancy model

## ESTIMATE DISEASE PREVALENCE

### Reality:

- Most tests are imperfect
- Result in occupancy/prevalence estimates that are biased low
- Underestimation of pathogen transmission rates
- Flawed predictions regarding infection dynamics and

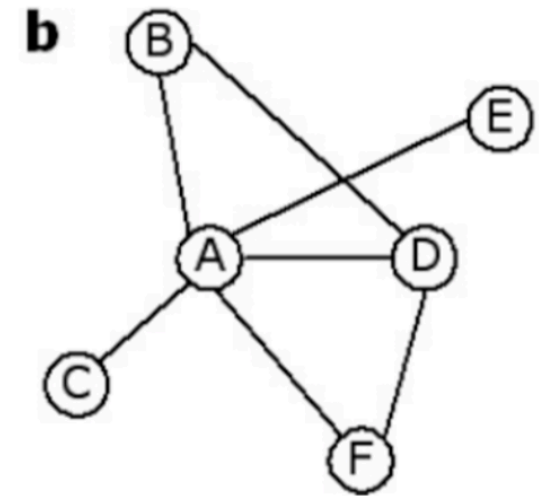
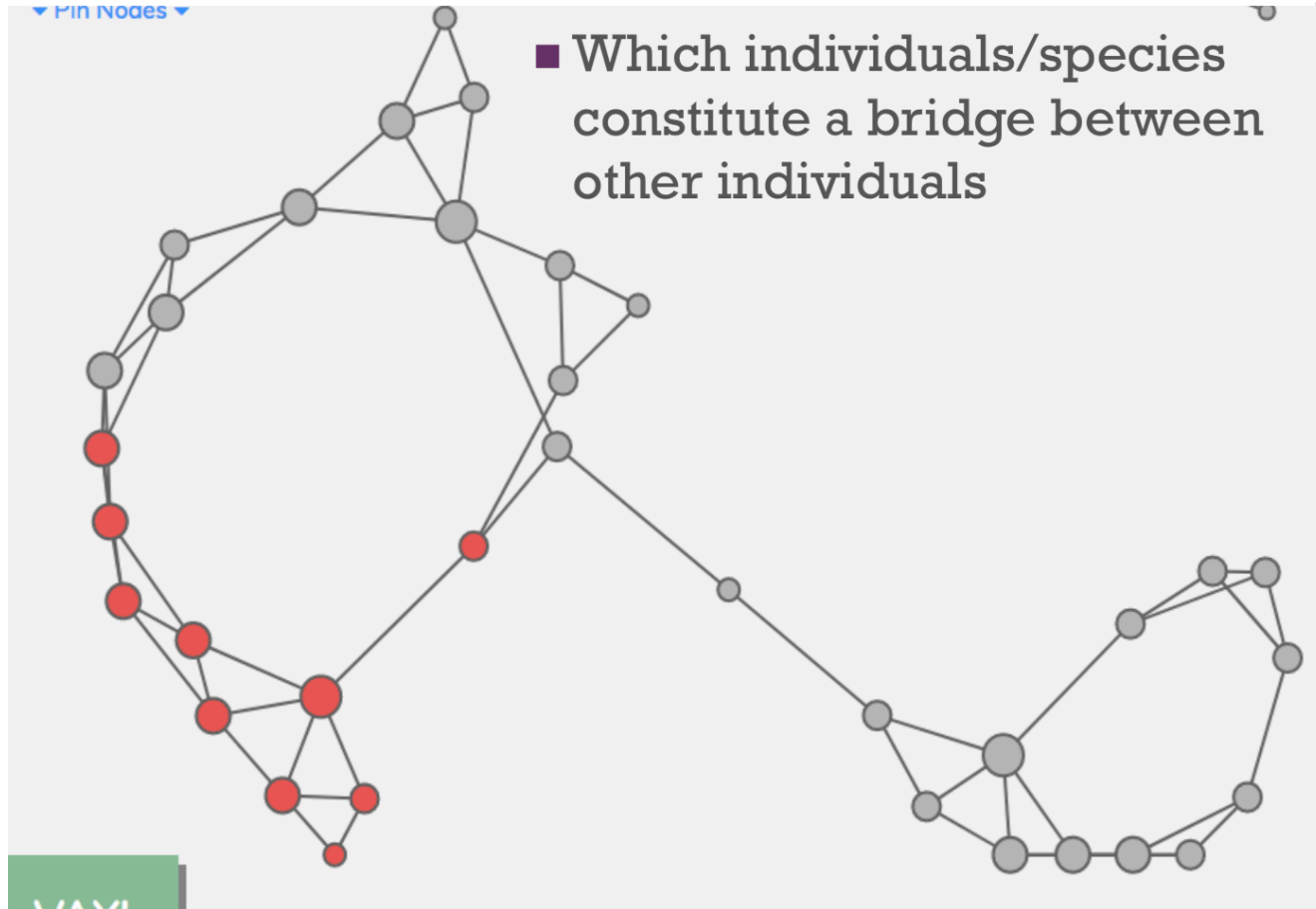


		DISEASE	
		Present	Absent
TEST	Positive	True positive a	False positive b
	Negative	False negative c	True negative d

## SINGLE SEASON OCCUPANCY

		Tested once	Occupancy
	n	Prevalence (95% CI)	
<i>Galidia</i>	29	0.48 (0.30-0.67)	0.83 (0.65-1.00)
<i>Galidictis</i>	12	0.92 (0.60-1.00)	1.00 (0.95-1.00)
Males	14	0.36 (0.14-0.64)	0.79 (0.54-1.00)
Females	27	0.48 (0.29-0.68)	0.94 (0.78-1.00)
Total	41	0.44 (0.29-0.60)	0.89 (0.72-1.00)

# Network



Individual	Degree
A	4
B	2
C	1
D	3
E	1
F	2

# Mechanistic models Occupancy models

Univariate  
linear

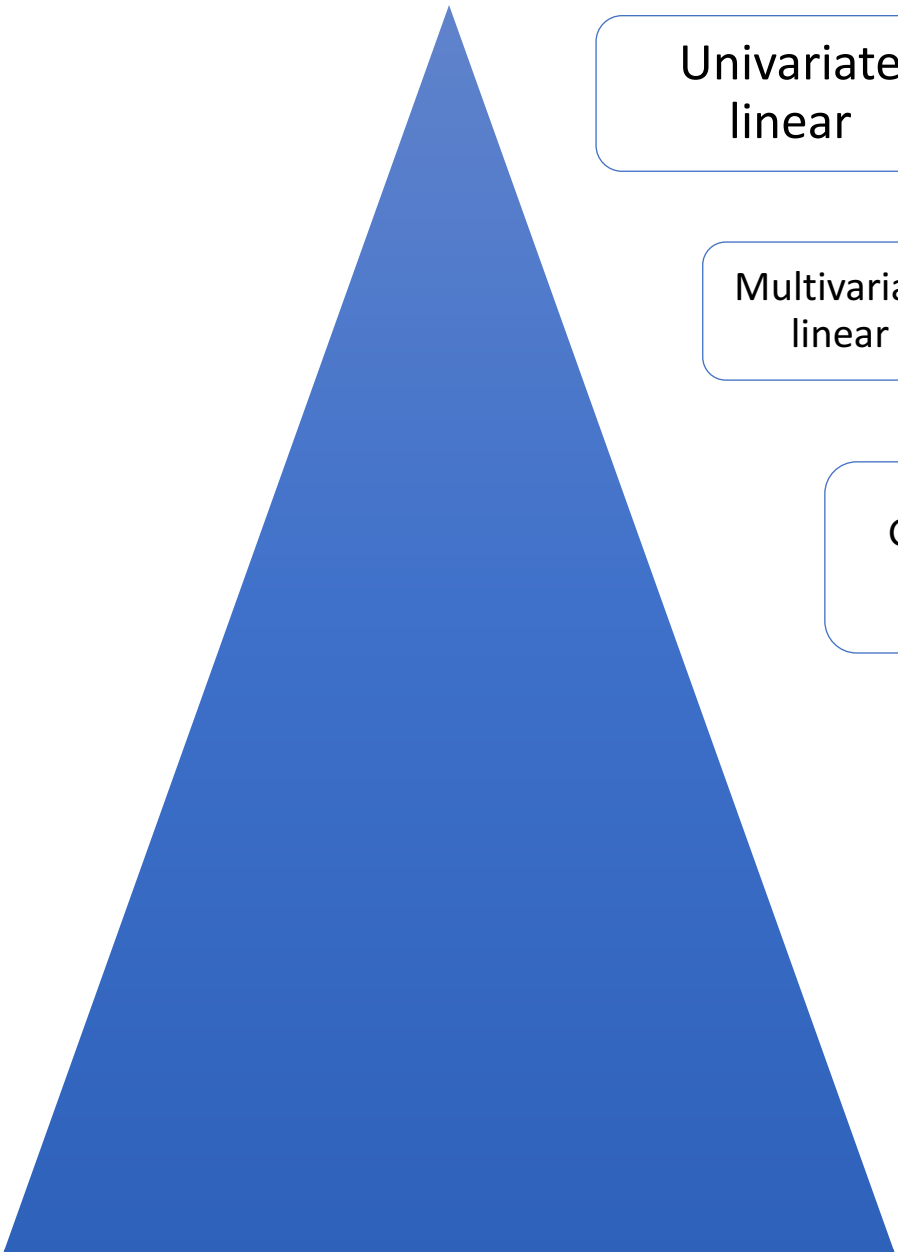
Multivariate  
linear

Generalized  
linear

Generalized linear  
and mixed

Network  
modeling

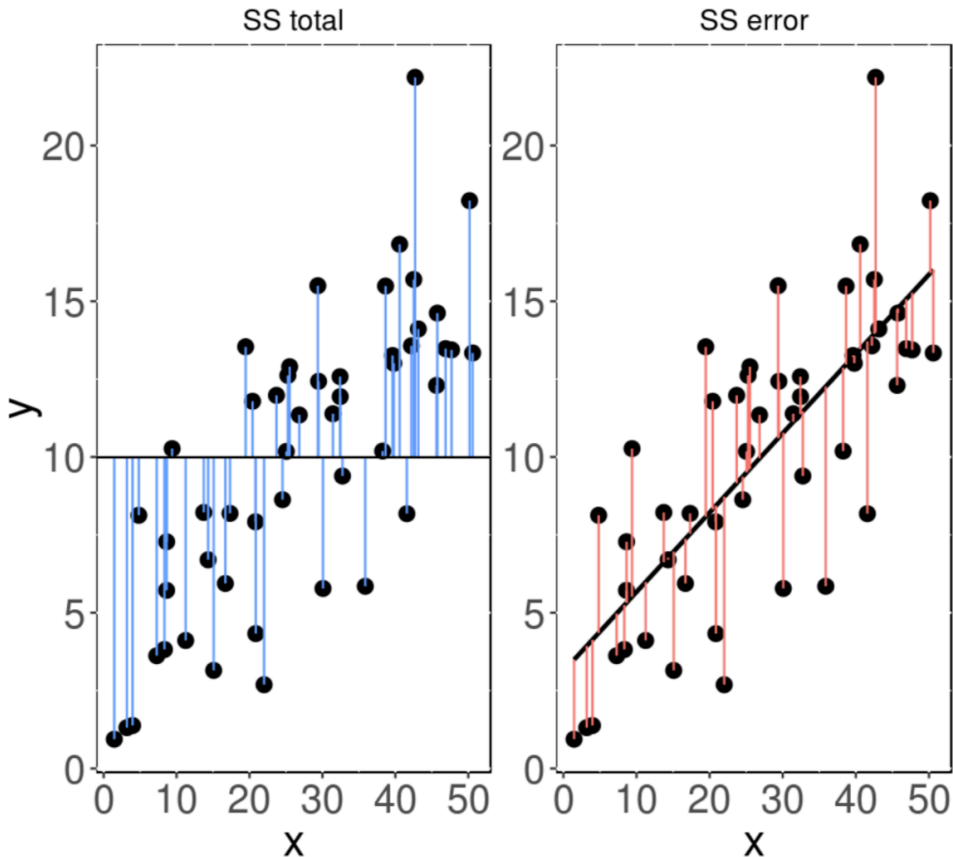
Increasing realism  
Decreasing tractability





# Model fitting

## Least square



## Maximum likelihood

Mathematical statements of all detection histories are combined into model likelihood, such as:

$$L(\psi, p | H_1, \dots, H_{30}) = \prod_{i=1}^{30} \Pr(H_i)$$

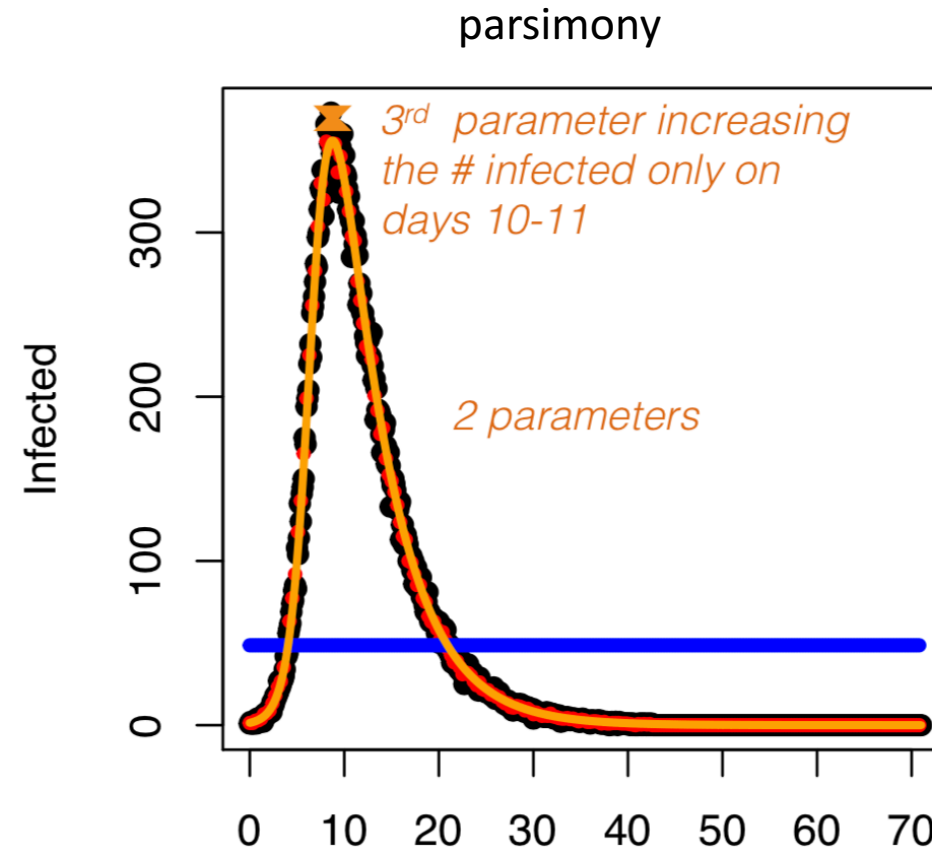
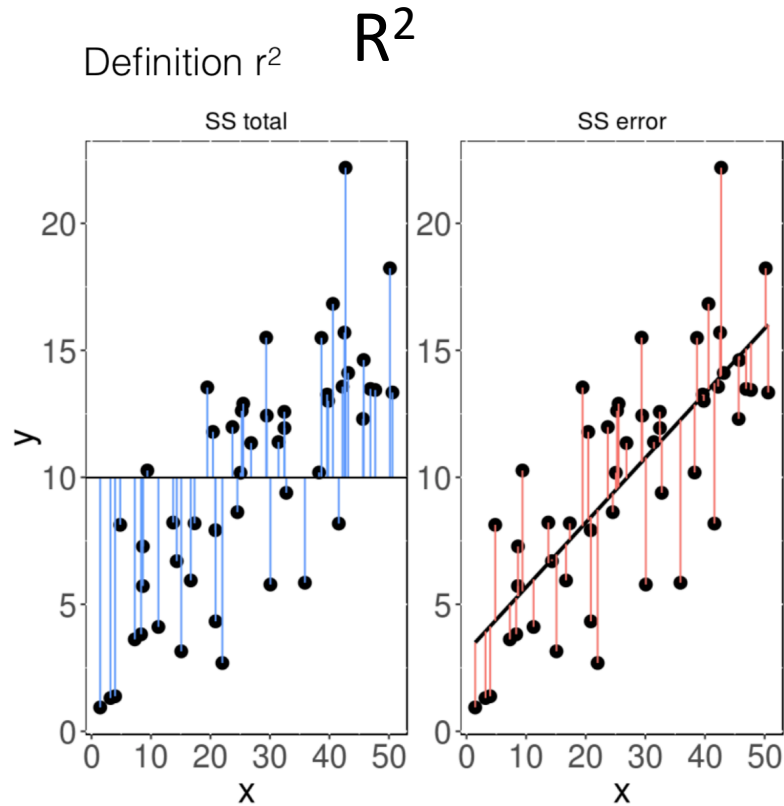
Product of math equations forms the model likelihood for the observed data

Using MLE determine  $\Psi$  and  $p$

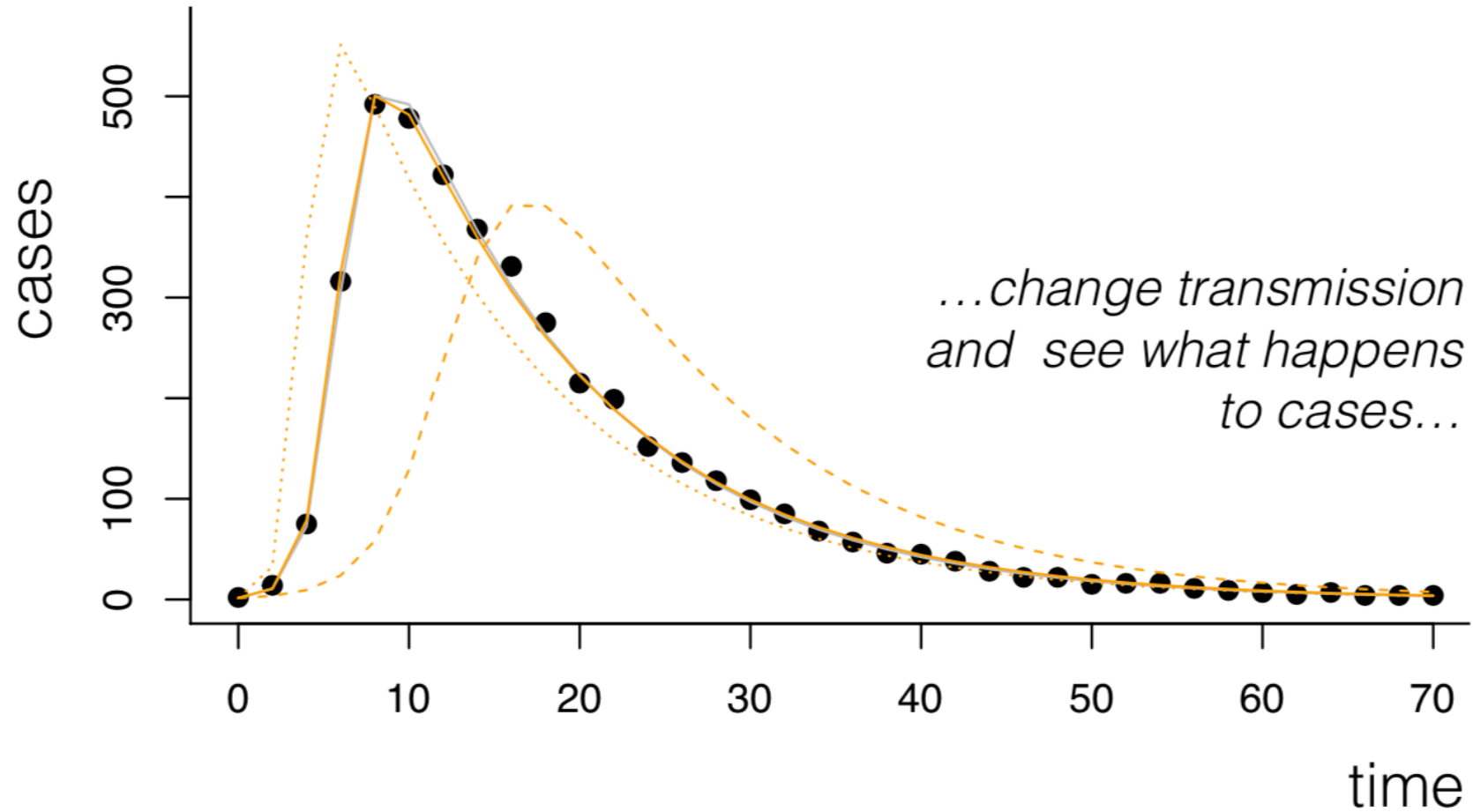
# Model fitting



# Model evaluation and comparison



# Sensitivity analyses



# Outline

- Science: research question
- Mechanistic model
- Statistical model
- R



# Basics

```
# In R you can assign a value to a variable by using the "<-" operator.  
# Run the following line of code by pressing "Control+Enter"
```

```
x <- 10
```

```
(1242-241.1)*32.21
```

```
# When you press control+Enter, the cursor automatically  
# runs the code in the console. This way, you can run scripts or  
# press control+enter.
```

```
# The following code does some basic arithmetic.
```

```
x <- 2          # ask someone to guess a number  
y <- x*9        # tell them to multiply it by 9  
d1 <- floor(y/10) # get the first digit (floor(x/10))  
d2 <- y%%10     # get the second digit (a%%b gives the remainder of a divided by b)  
d1+d2-4        # tell them to add the digits and subtract 4
```

```
# Indeed we can make a new list by using the "c" (concatenate) command:
```

```
mylist <- c(1.1, 2.2, 3.3, 4.4, 5.5, 4.4, 3.3, 2.2, 1.1)
```

```
require("Matrix")
```

```
# once you've included a package, you can use it  
# package. You can click the name of a package in the  
# help for that specific package. Here's an example of  
# package
```

```
M <- Matrix(0, 2, 2, sparse=FALSE)  
M[1,1] = 2; M[1,2] = 3  
M[2,1] = 3; M[2,2] = 4;  
M  
det(M)
```

# Intermediate

```
## ----Popdata, include=TRUE-----  
setwd("/Users/jessicametcalfe/Downloads/E2M2-Dropbox-2018/E2M2.Metcalfe.Lectures/Rcode/")  
pop.data <- read.csv("WorldBankPop.csv")  
head(pop.data[,1:10])
```

```
##### Arrange data #####  
## For this we will need the package "dplyr"  
## If you do have this packages yet, install it with the function  
"install.packages(...)"
```

```
install.packages("dplyr")  
install.packages("ggplot2")
```

```
## Then load it with require() or library()
```

```
require(dplyr)  
require(ggplot2)
```

```
> a + 1  
Error: object 'a' not found  
>
```

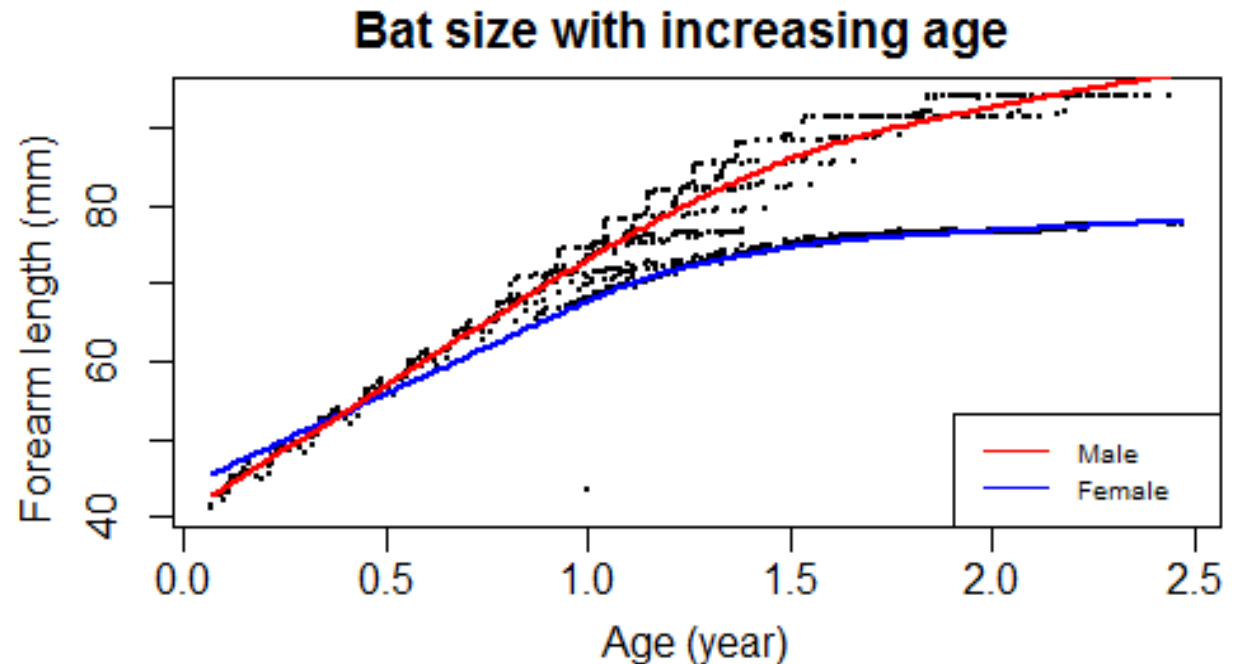


# Intermediate

```
#-----  
# 1. Data exploration: Plots and summary statistics  
#-----  
  
# Distribution of outcome variable  
hist(csb.data$outpatient, col='grey', main='', xlab='Number of outpatient visits per month')  
  
# Outpatient visits for each health center (exploration of association for categorical variables)  
boxplot(csb.data$outpatient~csb.data$csb, ylab='Number of outpatient visits per month')  
  
# Outpatient visits after interventions were in place  
boxplot(csb.data$outpatient~csb.data$int1, ylab='Number of outpatient visits per month')  
boxplot(csb.data$outpatient~csb.data$int2, ylab='Number of outpatient visits per month')  
  
# Correlation plots (exploration of association for quantitative variables)  
plot(csb.data$staff, csb.data$outpatient, ylab='Number of outpatient visits per month')  
abline(lm(outpatient~staff, data=csb.data))  
plot(csb.data$ref, csb.data$outpatient, ylab='Number of outpatient visits per month')  
abline(lm(outpatient~ref, data=csb.data))  
  
# We'll check a multivariate model that includes number of medical staff and  
# (we don't consider a full model for simplicity and lack of sufficient observ  
m1=glmer.nb(outpatient~ staff+ int1+ int2+ season+ (1 | csb), data=csb.data )  
summary(m1)  
|
```

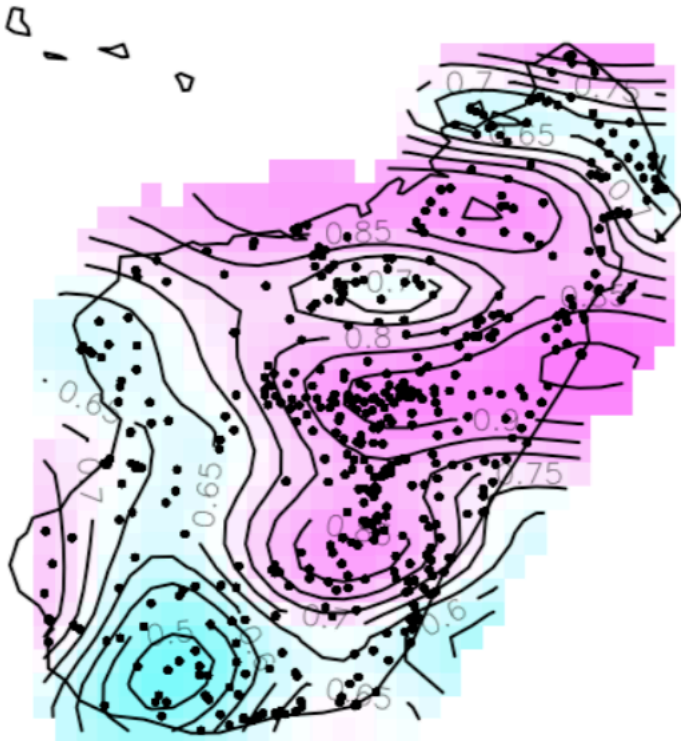
# Intermediate

```
# The variable "Number of parasites" is count data and it's poisson dist  
# This type of variable is typically modelled with poisson models  
m6=glm(GIparasites~age+sexe+malaria, family='poisson', data=lemur.data)  
summary(m6)  
  
m7=step(m6)  
summary(m7)
```

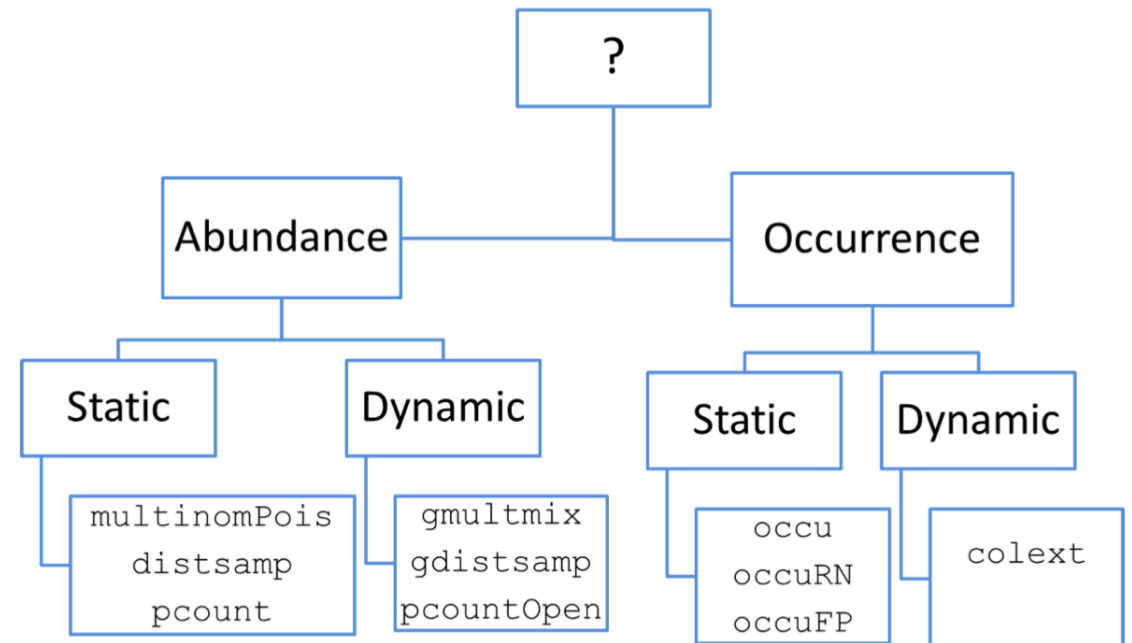


# Advanced

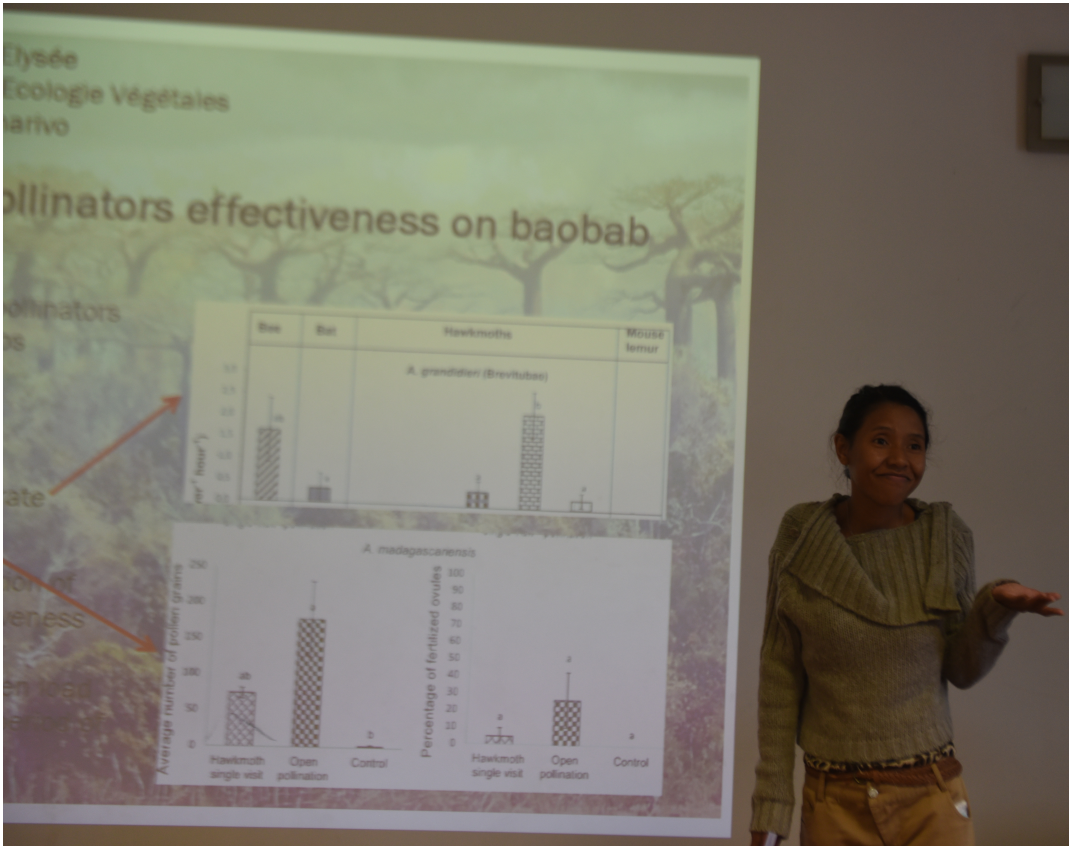
Add dsolve for LV model



**WHICH MODEL SHOULD I  
USE (UNMARKED)?**



# Project presentation and completion



## Manuscript writing and submission

- What are the main results that provide the answer to my question?
  - 1 to 3 graphs
  - 1 to 3 tables
- What is the journal that best fits my study?
  - Scope, audience, impact factor, math focus
- How do I present my manuscript?
  - Introduction: set the stage to your question
  - Methodology: describe explicitly all steps for replicability
  - Results: clear and concise
  - Discussion: explain how your study improves previous knowledge

You are now well equipped!





Any aminareo ny baolina!

